**Purpose:** In this problem set, you will review and practice graphing polynomials by analyzing formulas and practice finding possible formulas for a given graph.

- 1. For each function below, describe the end behavior.
  - (a)  $f(x) = x^2 + 4x + 3$
  - (b)  $g(x) = -x^3 + 9x^2 24x 1$
  - (c)  $h(x) = x^3 + 3$
  - (d)  $P(x) = x^4 + x^3 + 1$

(e) 
$$Q(x) = -x^2 + 1$$

2. Find the zeros of the polynomials below and their multiplicities.

(a) 
$$f(x) = -2(x-1)(x+2)^2(x+5)^3$$

(b) 
$$g(x) = x^2 - 3x + 2$$

(c) 
$$h(x) = (3x+5)(x-3)$$

3. Match the functions with their graphs.



$$f(x) = -x^{4} + 1$$

$$f(x) = x^{5} - 5x^{3} + 4x$$

$$f(x) = x^{3}$$

$$f(x) = x^{6} - 6x^{4} + 9x^{2}$$

$$f(x) = -x^{3} + x^{2} + 2x$$

4. Consider the polynomial  $f(x) = (x^2 - 4)(x - 1)$ .



- (a) Find the roots and the *y*-intercept of the polynomial. Label these on the graph.
- (b) Describe the end behavior of the polynomial. Identify these on the graph.
- (c) Does the polynomial have any local extrema? Identify them on the graph above and classify each as a maximum or minimum.
- (d) Using the graph above, estimate the intervals of increase and decrease. Label these on the graph.

5. Sketch the graph of  $f(x) = x^4 + x^3$ .