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Precalculus
Purpose: In this problem set, you will review and practice graphing polynomials by analyzing formulas and practice finding possible formulas for a given graph.

1. For each function below, describe the end behavior.
(a) $f(x)=x^{2}+4 x+3$
(b) $g(x)=-x^{3}+9 x^{2}-24 x-1$
(c) $h(x)=x^{3}+3$
(d) $P(x)=x^{4}+x^{3}+1$
(e) $Q(x)=-x^{2}+1$
2. Find the zeros of the polynomials below and their multiplicities.
(a) $f(x)=-2(x-1)(x+2)^{2}(x+5)^{3}$
(b) $g(x)=x^{2}-3 x+2$
(c) $h(x)=(3 x+5)(x-3)$
3. Match the functions with their graphs.



$\ldots f(x)=-x^{4}+1$
$\ldots f(x)=x^{5}-5 x^{3}+4 x$
$\ldots f(x)=x^{3}$
$\ldots f(x)=x^{6}-6 x^{4}+9 x^{2}$
$\ldots f(x)=-x^{3}+x^{2}+2 x$
4. Consider the polynomial $f(x)=\left(x^{2}-4\right)(x-1)$.

(a) Find the roots and the $y$-intercept of the polynomial. Label these on the graph.
(b) Describe the end behavior of the polynomial. Identify these on the graph.
(c) Does the polynomial have any local extrema? Identify them on the graph above and classify each as a maximum or minimum.
(d) Using the graph above, estimate the intervals of increase and decrease. Label these on the graph.
5. Sketch the graph of $f(x)=x^{4}+x^{3}$.

